

59. The transverse displacement at position x and time t in a string due to a travelling wave is given by $y(x, t) = 3.0 \cos(\pi x - 4\pi t)$ cm, where x is in centimeters and t is in seconds. Which of the following statements is wrong?

- A Maximum value of transverse velocity of any point is 12π cm/s and wavelength is 0.2 m.
- B Speed of wave propagation in the +ve x -direction is 4π cm/s.
- C Transverse velocity at $t = 0$ and $x = 0.25$ cm is $6\sqrt{2}\pi$ cm/s.
- D Maximum value of transverse acceleration of any point is $48\pi^2$ cm/s².

$$y(x, t) = A \cos(kx - \omega t), \quad k = \frac{2\pi}{\lambda} \quad A = \text{amplitude.}$$

Transverse Velocity $\left(\frac{dy}{dt}\right)_{x \text{ as a constant}} = \frac{\partial y}{\partial t} = A \times -\sin(kx - \omega t) \times -\omega$

$$= A\omega \sin(kx - \omega t)$$

$$\therefore (V_{\text{trans}})_{\text{max}} = A\omega$$

Transverse Acceleration $= \frac{\partial^2 y}{\partial t^2} = -A\omega^2 \cos(kx - \omega t)$

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$$3.0 \cos(\pi x - 4\pi t) \text{ cm,}$$

$$A = 3 \text{ cm}$$

$$\pi = k = \frac{2\pi}{\lambda}$$

$$\therefore \lambda = 2 \text{ cm}$$

$$\omega = 4\pi \text{ rad/s}$$

$$f = \frac{\omega}{2\pi} = 2 \text{ Hz.}$$

D $A\omega^2 = 3 \times (4\pi)^2 = 3 \times 16 \times \pi^2 = 48\pi^2$ ✓

C $A\omega \sin(kx - \omega t)$ ✓

$$v_1 = 3 \times 4\pi \times \sin\left(\pi x - 4\pi t\right)$$

$$= 12\pi \times \sin\left(\frac{\pi}{4} - 0\right) = \frac{12\pi}{\sqrt{2}}$$

$$= 6\sqrt{2}\pi \text{ cm/s.}$$

B $v = \lambda f = 2 \times 2 = 4 \text{ cm/s. NOT } 4\pi \text{ cm/s.}$

- A Maximum value of transverse velocity of any point is 12π cm/s and wavelength is 0.2 m.

$$\lambda = 0.02 \text{ m.}$$

$$(V_{\text{trans}})_{\text{max}} = A\omega = 3 \times 4\pi = 12\pi \text{ cm/s.}$$